

AP Calculus AB

The Accumulation Function

$$1) g(x) = \int_0^x f(t) dt$$

$$a) g(0) = 0$$

$$b) g(1) = \frac{1}{2}(1)(3)$$

$$c) g(2) = 0$$

$$d) g(-2) = 0$$

$$2) g(x) = 2x + \int_0^x f(t) dt$$

$$a) g(0) = 0$$

$$b) g(3) = 6 + \int_0^3 f(t) dt = 6$$

$$c) g(-3) = -6 + \int_0^{-3} f(t) dt$$

$$= -6 - \frac{1}{4} \pi(9) = -6 - \frac{9\pi}{4}$$

$$d) g(-4) = -8 + \int_0^{-4} f(t) dt$$

$$= -8 - \frac{9\pi}{4} + \frac{1}{4} \pi = -8 - 2\pi$$

$$3) g(x) = 5 + \int_0^x f(t) dt$$

$$a) g(3) = 5 + \int_0^3 f(t) dt$$

$$= 5 + \frac{1}{4} \pi(2)^2 + \frac{1}{2}(1)(3)$$

$$= \frac{13}{2} + \pi$$

$$b) g(-2) = 5 + \int_0^{-2} f(t) dt$$

$$= 5 - \pi$$

$$c) g(5) = 5 + \int_0^5 f(t) dt$$

$$= 5 + \pi + \frac{1}{2} \left(\frac{5}{2} \right) (3) - \frac{1}{2} \left(\frac{1}{2} \right) (1)$$

$$= \frac{17}{2} + \pi$$

$$5) \int_1^2 (x^2 + 3x - 2) dx$$

$$\left. \frac{1}{3} x^3 + \frac{3}{2} x^2 - 2x + C \right|_1^2$$

$$\left(\frac{8}{3} + 6 - 4 \right) - \left(\frac{1}{3} + \frac{3}{2} - 2 \right)$$

$$4) g(x) = \int_1^x f(t) dt$$

$$a) g(0) = \int_1^0 f(t) dt = 1$$

$$b) g(5) = \int_1^5 f(t) dt$$

$$= 3$$

$$c) g(-3) = -1$$

$$6) \int_0^{\pi} \sin x dx = -\cos x + C \Big|_0^{\pi}$$

$$(-\cos \pi) - (-\cos 0)$$

$$1 + 1$$

$$\boxed{2}$$

